# Package: FlexVarJM (via r-universe)

September 17, 2024

Title Estimate Joint Models with Subject-Specific Variance

Version 0.1.0

**Description** Estimation of mixed models including a subject-specific variance which can be time and covariate dependent. In the joint model framework, the package handles left truncation and allows a flexible dependence structure between the competing events and the longitudinal marker. The estimation is performed under the frequentist framework, using the Marquardt-Levenberg algorithm. (Courcoul, Tzourio, Woodward, Barbieri, Jacqmin-Gadda (2023) <arXiv:2306.16785>).

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**Encoding** UTF-8

**Roxygen** list(markdown = TRUE)

RoxygenNote 7.2.3

**Imports** ggplot2, lcmm, marqLevAlg, mvtnorm, randtoolbox, Rcpp, stats, survminer, utils

Depends R (>= 3.5.0), splines, survival

URL https://github.com/LeonieCourcoul/FlexVarJM

BugReports https://github.com/LeonieCourcoul/FlexVarJM/issues

LazyData true

Suggests knitr, rmarkdown

VignetteBuilder knitr

LinkingTo Rcpp, RcppArmadillo

Repository https://leoniecourcoul.r-universe.dev

RemoteUrl https://github.com/leoniecourcoul/flexvarjm

RemoteRef HEAD

RemoteSha 599c1addcdea841ac4327a300eb58e7c339dd79d

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data.GaussKronrod Initialisation of Survival Data at Gauss Kronrod time points

# Description

Initialisation of Survival Data at Gauss Kronrod time points

# Usage

```
data.GaussKronrod(data.id, Time, k = 15)
```

# Arguments

| data.id | A database with covariates of interest and 1 line per subject |
|---------|---|
| Time    | A vector of time event  |
| k       | The number of Gauss Kronrod points, by default $k = 15$       |

### Value

A list with the following components :

- K an integer, the number of points
- P a vector, of value Time/2
- st a matrix with nrow = number of subjects and ncol = k. The new time to compute the survival function

wk a vector of weights

data.id2 a database with K lines per subjects

id.GK the vector of IDs

data.GaussKronrod2 Initialisation of Survival Data at Gauss Kronrod time points 2

### Description

Initialisation of Survival Data at Gauss Kronrod time points 2

### Usage

```
data.GaussKronrod2(data.id, a, b, k = 15)
```

### Arguments

| data.id | A database with covariates of interest and 1 line per subject |
|---------|---|
| а       | First born  |
| b       | Second born   |
| k       | The number of Gauss Kronrod points, by default $k = 15$       |

### Value

A list with the following components :

- K an integer, the number of points
- P a vector, of value Time/2
- st a matrix with nrow = number of subjects and ncol = k. The new time to compute the survival function
- wk a vector of weights
- data.id2 a database with K lines per subjects
- id.GK the vector of IDs

data.manag.long

### Description

Management of longitudinal data

### Usage

data.manag.long(formGroup, formFixed, formRandom, data.long1)

### Arguments

| formGroup  | A formula which indicates the group variable                               |
|------------|--|
| formFixed  | A formula which indicates the fixed effects for the longitudinal submodel  |
| formRandom | A formula which indicates the random effects for the longitudinal submodel |
| data.long1 | A dataframe with the longitudinal data                                     |

### Value

A list with the following components :

data\_long a clean dataframe for the longitudinal data

- y.new.prog the vector of responses variable
- X a matrix with the fixed effects
- U a matrix with the random effects
- id a vector with the identification of individuals
- offset a vector with the number of measurements for each individual
- I an integer, the number of individuals

data.manag.surv Management of survival data

### Description

Management of survival data

### Usage

```
data.manag.surv(formGroup, formSurv, data.long1, formSurv_CompRisk)
```

### data.time

### Arguments

| formGroup         | A formula which indicates the group variable                                |  |
|-------------------|---|--|
| formSurv          | A formula which indicates the variables used in the survival submodel       |  |
| data.long1        | Database  |  |
| formSurv_CompRisk |   |  |
|                   | A formula which indicates the variables used in the competing survival sub- |  |
|                   | model   |  |

### Value

A list with the following components :

tmp the final database for survival analysis

Time a vector of observed times

event1 a vector of first event indicator

nTime length of Time vector

Z matrix of covariables of first survival submodel

event2 a vector of second event indicator

Z\_CR matrix of covariables of second survival submodel

data.time

Management of data for longitudinal submodel

# Description

Management of data for longitudinal submodel

## Usage

data.time(data.id, Time, formFixed, formRandom, timeVar)

### Arguments

| data.id    | A dataframe  |
|------------|--|
| Time       | A vector of Time of events   |
| formFixed  | A formula for the fixed effects of the longitudinal submodel                     |
| formRandom | A formula for the random effects of the longitudinal submodel                    |
| timeVar    | The name of the column of time in data.id. This variable must appears in data.id |

### Value

A list with the following components

Xtime a matrix of fixed effects at each time of measure

Utime a matrix of random effects at each time of measure

Data\_toy

### Description

A simulated dataset for the example of the FlexVarJM package.

### Usage

Data\_toy

### Format

A data frame with 2076 rows and 5 variables:

ID the Id of each subject

visit the time of measurement

 $\mathbf{y}$  the value of the marker

time the time of the first event observed

event the first event observed : 0 =censoring, 1 =first event, 2 = second event

gaussKronrod Gauss-Kronrod nodes and weights

### Description

Gauss-Kronrod nodes and weights

### Usage

gaussKronrod(k = 15)

### Arguments

k

the number of points for Gauss-Kronrod approximation : choice between 7 and 15. 15 by default.

### Value

A list with the following components :

sk A k-vector of nodes

wk A k-vector of weights

| <pre>goodness_of_fit</pre> | Predictions for the goodness of fit, of the random effects, the current |
|----------------------------|---|
|                            | value for each individuals and the cumulative hazard function for both  |
|                            | events  |

### Description

Predictions for the goodness of fit, of the random effects, the current value for each individuals and the cumulative hazard function for both events

### Usage

```
goodness_of_fit(object, graph = FALSE, break.times = NULL)
```

### Arguments

| object      | an object of class lsjm                                       |
|-------------|---|
| graph       | a boolean to indicate to print graphics, False by default     |
| break.times | a vector of times for the time points of longitudinal graphic |

### Value

A list which contains the following elements :

tables A list with the table of the predicted random effect, the table of the predicted current value, table(s) of predictive cumulative hazard function(s)

graphs A list with 2 or 3 graphs : one for the longitudinal adjustment and one for each risk function

### Examples

```
#Fit a joint model with competing risks and subject-specific variability
example <- lsjm(formFixed = y~visit,
formRandom = ~ visit,
formGroup = ~ID,
formSurv = Surv(time, event ==1 ) ~ 1,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
sharedtype = c("current value", "variability"),
hazard_baseline = "Weibull",
formSlopeFixed =~1,
formSlopeRandom = ~1,</pre>
```

```
indices_beta_slope = c(2),
competing_risk = TRUE,
formSurv_CR = Surv(time, event ==2 ) ~ 1,
hazard_baseline_CR = "Weibull",
sharedtype_CR = c("current value", "variability"),
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100,
Comp.Rcpp = TRUE
)
#Assesment of the goodness of fit:
gof <- goodness_of_fit(example, graph = TRUE)
gof$tables
gof$graphs
```

initial.long Initialisation of Longitudinal Submodel

### Description

Initialisation of Longitudinal Submodel

### Usage

```
initial.long(formFixed, formRandom, idVar, data.long1, ncX, nproc = nproc)
```

### Arguments

| formFixed  | A formula which indicates the fixed effects for the longitudinal submodel      |
|------------|--|
| formRandom | A formula which indicates the random effects for the longitudinal submodel     |
| idVar      | A character, indicates the name of the group variable                          |
| data.long1 | A dataframe with the longitudinal data   |
| ncX        | An integer, the number of columns of matrix X, ie, the number of fixed effects |
| nproc      | An integer, the number of cores for parallel computation                       |

### Value

A list with the following components :

long\_model the result of the hlme function

priorMean.beta the estimated parameters for fixed effects in the linear mixed effects model sigma the estimated sigma of the model

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log\_llh

# Description

Log-likelihood computation

### Usage

log\_llh( param, nb.e.a, nb.priorMean.beta, nb.alpha, competing\_risk, nb.alpha.CR, variability\_hetero, S, Zq, sharedtype, sharedtype\_CR, hazard\_baseline, hazard\_baseline\_CR, ord.splines, Xtime, Utime, nb\_pointsGK, Xs, Us, Xslope, Uslope, Xs.slope, Us.slope, indices\_beta\_slope, Time, st\_calc, Β, Bs, wk, Ζ, Ρ, left\_trunc, Z\_CR, X\_base, offset, U, y.new.prog,

```
event1,
  event2,
  Ind,
 Xs.0,
 Us.0,
 Xs.slope.0,
 Us.slope.0,
 P.0,
  st.0,
 Bs.0,
 B.CR,
 Bs.CR,
 Bs.0.CR,
 nb.e.a.sigma = nb.e.a.sigma,
  nb.omega = nb.omega,
 Otime = Otime,
 Wtime = Wtime,
 0s = 0s,
 Ws = Ws,
 0_base = 0_base,
 W_base = W_base,
 correlated_re = correlated_re,
 0s.0 = 0s.0,
 Ws.0 = Ws.0
)
```

## Arguments

| param                     | a vector : paramaters to be estimated   |
|---------------------------|---|
| nb.e.a                    | integer : number of RE  |
| nb.priorMean.be           | ta  |
|                           | integer : number of fixed effects   |
| nb.alpha                  | integer : number of covariates in survival model  |
| <pre>competing_risk</pre> | boolean : allow competing risk or not, FALSE by default   |
| nb.alpha.CR               | integer : number of covariates in survival model for competing risks  |
| variability_het           | ero   |
|                           | boolean : allow the heterogeneous variability or not  |
| S                         | integer : the number of QMC points  |
| Zq                        | vector : sobol points   |
| sharedtype                | vector : dependence structure for survival model : "RE" (random effects) or "CV" (current value) or "CVS" (current value and slope) or "S" (slope)                |
| sharedtype_CR             | vector : dependence structure for competing risk survival model : "RE" (random effects) or "CV" (current value) or "CVS" (current value and slope) or "S" (slope) |
| hazard_baseline           |   |
|                           | char : baseline hazard function : "Exponential" or "Weibull" or "Splines"   |

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# log\_llh

| hazard_baseline_CR |   |
|--------------------|---|
|                    | char : baseline hazard function, competing risk : "Exponential" or "Weibull" or "Splines" |
| ord.splines        | integer : the order of splines function for baseline hazard function                      |
| Xtime              | matrix : fixed effects at event time  |
| Utime              | matrix : RE at event time   |
| nb_pointsGK        | integer : number of points for Gauss-Kronrod approximation, 7 or 15 (default)             |
| Xs                 | matrix : fixed effects at Gauss-Kronrod times   |
| Us                 | matrix : RE at Gauss-Kronrod times  |
| Xslope             | matrix : fixed effects of slope at event times  |
| Uslope             | matrix : RE of slope at event times   |
| Xs.slope           | matrix : fixed effects of slope at Gauss-Kronrod times                                    |
| Us.slope           | matrix : RE of slope at Gauss-Kronrod times   |
| indices_beta_s     |   |
|                    | vector : position of beta which will be used in the slope computation                     |
| Time               | vector : observed event times   |
| st_calc            | matrix : Gauss-Kronrod times  |
| В                  | matrix : splines for baseline hazard function of event 1                                  |
| Bs                 | matrix : splines for baseline survival function of event 1                                |
| wk                 | vector : Gauss-Kronrod weights  |
| Z                  | matrix : covariates for survival function of event 1                                      |
| Р                  | vector : Time/2   |
| left_trunc         | boolean : left truncation indicator   |
| Z_CR               | matrix : covariates for survival function of event 2                                      |
| X_base             | matrix : fixed effects for longitudinal submodel  |
| offset             | vector : number of lines per subjects   |
| U                  | matrix : RE for longitudinal submodel   |
| y.new.prog         | vector : y measures for longitudinal submodel   |
| event1             | vector : event 1 indicator  |
| event2             | vector : event 2 indicator  |
| Ind                | integer : number of subjects  |
| Xs.0               | same for left truncation  |
| Us.0               | same for left truncation  |
| Xs.slope.0         | same for left truncation  |
| Us.slope.0         | same for left truncation  |
| P.0                | same for left truncation  |
| st.0               | same for left truncation  |
| Bs.0               | same for left truncation  |
|                    |   |

| B.CR          | same for left truncation   |
|---------------|--|
| Bs.CR         | same for left truncation   |
| Bs.0.CR       | same for left truncation   |
| nb.e.a.sigma  | integer : number of RE for variability                               |
| nb.omega      | integer : number of fixed effects for variability                    |
| Otime         | matrix : fixed effects of variability at event time                  |
| Wtime         | matrix : RE of variability at event time                             |
| 0s            | matrix : fixed effects of variability at Gauss-Kronrod times         |
| Ws            | matrix : random effects of variability at Gauss-Kronrod times        |
| 0_base        | matrix : fixed effects for variability                               |
| W_base        | matrix : fixed effects for variability                               |
| correlated_re | boolean : indicator to allow all the random effects to be correlated |
| 0s.0          | matrix : same for left truncation                                    |
| Ws.0          | matrix : same for left truncation                                    |

### Value

The value of the log-likelihood

log\_llh\_rcpp Log-likelihood computation in RCPP

# Description

Log-likelihood computation in RCPP

# Usage

```
log_llh_rcpp(
  param,
  nb.e.a,
  nb.priorMean.beta,
  nb.alpha,
  competing_risk,
  nb.alpha.CR,
  variability_hetero,
  S,
  Zq,
  sharedtype,
  sharedtype_CR,
  hazard_baseline,
  hazard_baseline_CR,
  ord.splines,
```

Xtime, Utime, nb\_pointsGK, Xs, Us, Xslope, Uslope, Xs.slope, Us.slope, indices\_beta\_slope, Time, st\_calc, Β, Bs, wk, Ζ, Ρ, left\_trunc, Z\_CR, X\_base, offset, U, y.new.prog, event1, event2, Ind, Xs.0, Us.0, Xs.slope.0, Us.slope.0, P.0, st.0, Bs.0, B.CR, Bs.CR, Bs.0.CR, nb.e.a.sigma = nb.e.a.sigma, nb.omega = nb.omega, Otime = Otime, Wtime = Wtime, 0s = 0s, Ws = Ws, 0\_base = 0\_base, W\_base = W\_base, correlated\_re = correlated\_re, 0s.0 = 0s.0, Ws.0 = Ws.0)

# Arguments

| param              | a vector : paramaters to be estimated   |  |
|--------------------|---|--|
| nb.e.a             | integer : number of RE  |  |
| nb.priorMean.be    |   |  |
|                    | integer : number of fixed effects   |  |
| nb.alpha           | integer : number of covariates in survival model  |  |
| competing_risk     | boolean : allow competing risk or not, FALSE by default   |  |
| nb.alpha.CR        | integer : number of covariates in survival model for competing risks  |  |
| variability_het    |   |  |
|                    | boolean : allow the heterogeneous variability or not  |  |
| S                  | integer : the number of QMC points  |  |
| Zq                 | vector : sobol points   |  |
| sharedtype         | vector : dependence structure for survival model : "RE" (random effects) or<br>"CV" (current value) or "CVS" (current value and slope) or "S" (slope)                     |  |
| sharedtype_CR      | vector : dependence structure for competing risk survival model : "RE" (ran-<br>dom effects) or "CV" (current value) or "CVS" (current value and slope) or "S"<br>(slope) |  |
| hazard_baseline    |   |  |
|                    | char : baseline hazard function : "Exponential" or "Weibull" or "Splines"   |  |
| hazard_baseline    | e_CR<br>char : baseline hazard function, competing risk : "Exponential" or "Weibull" or   |  |
|                    | "Splines"   |  |
| ord.splines        | integer : the order of splines function for baseline hazard function  |  |
| Xtime              | matrix : fixed effects at event time  |  |
| Utime              | matrix : RE at event time   |  |
| nb_pointsGK        | integer : number of points for Gauss-Kronrod approximation, 7 or 15 (default)   |  |
| Xs                 | matrix : fixed effects at Gauss-Kronrod times   |  |
| Us                 | matrix : RE at Gauss-Kronrod times  |  |
| Xslope             | matrix : fixed effects of slope at event times  |  |
| Uslope             | matrix : RE of slope at event times   |  |
| Xs.slope           | matrix : fixed effects of slope at Gauss-Kronrod times  |  |
| Us.slope           | matrix : RE of slope at Gauss-Kronrod times   |  |
| indices_beta_slope |   |  |
|                    | vector : position of beta which will be used in the slope computation   |  |
| Time               | vector : observed event times   |  |
| st_calc            | matrix : Gauss-Kronrod times  |  |
| В                  | matrix : splines for baseline hazard function of event 1  |  |
| Bs                 | matrix : splines for baseline survival function of event 1  |  |
| wk                 | vector : Gauss-Kronrod weights  |  |
|                    |   |  |

| Z             | matrix : covariates for survival function of event 1                 |
|---------------|--|
| Р             | vector : Time/2  |
| left_trunc    | boolean : left truncation indicator                                  |
| Z_CR          | matrix : covariates for survival function of event 2                 |
| X_base        | matrix : fixed effects for longitudinal submodel                     |
| offset        | vector : number of lines per subjects                                |
| U             | matrix : RE for longitudinal submodel                                |
| y.new.prog    | vector : y measures for longitudinal submodel                        |
| event1        | vector : event 1 indicator   |
| event2        | vector : event 2 indicator   |
| Ind           | integer : number of subjects   |
| Xs.0          | same for left truncation   |
| Us.0          | same for left truncation   |
| Xs.slope.0    | same for left truncation   |
| Us.slope.0    | same for left truncation   |
| P.0           | same for left truncation   |
| st.0          | same for left truncation   |
| Bs.0          | same for left truncation   |
| B.CR          | same for left truncation   |
| Bs.CR         | same for left truncation   |
| Bs.0.CR       | same for left truncation   |
| nb.e.a.sigma  | integer : number of RE for variability                               |
| nb.omega      | integer : number of fixed effects for variability                    |
| Otime         | matrix : fixed effects of variability at event time                  |
| Wtime         | matrix : RE of variability at event time                             |
| Os            | matrix : fixed effects of variability at Gauss-Kronrod times         |
| Ws            | matrix : random effects of variability at Gauss-Kronrod times        |
| 0_base        | matrix : fixed effects for variability                               |
| W_base        | matrix : fixed effects for variability                               |
| correlated_re | boolean : indicator to allow all the random effects to be correlated |
| Os.0          | matrix : same for left truncation                                    |
| Ws.0          | matrix : same for left truncation                                    |

# Value

The value of the log-likelihood

 $\verb"log_llh_rcpp_cov"$ 

*Log-likelihood computation in RCPP with variance-covariance matrix for the random effects* 

# Description

Log-likelihood computation in RCPP with variance-covariance matrix for the random effects

### Usage

log\_llh\_rcpp\_cov( param, nb.e.a, nb.priorMean.beta, nb.alpha, competing\_risk, nb.alpha.CR, variability\_hetero, S, Zq, sharedtype, sharedtype\_CR, hazard\_baseline, hazard\_baseline\_CR, ord.splines, Xtime, Utime, nb\_pointsGK, Xs, Us, Xslope, Uslope, Xs.slope, Us.slope, indices\_beta\_slope, Time, st\_calc, Β, Bs, wk, Ζ, Ρ, left\_trunc, Z\_CR, X\_base, offset, U,

```
y.new.prog,
 event1,
 event2,
 Ind,
 Xs.0,
 Us.0,
 Xs.slope.0,
 Us.slope.0,
 P.0,
 st.0,
 Bs.0,
 B.CR,
 Bs.CR,
 Bs.0.CR,
 nb.e.a.sigma = nb.e.a.sigma,
 nb.omega = nb.omega,
 Otime = Otime,
 Wtime = Wtime,
 0s = 0s,
 Ws = Ws,
 0_base = 0_base,
 W_base = W_base,
 correlated_re = correlated_re,
 0s.0 = 0s.0,
 Ws.0 = Ws.0
)
```

# Arguments

| param              | a vector : paramaters to be estimated   |  |
|--------------------|---|--|
| nb.e.a             | integer : number of RE  |  |
| nb.priorMean.beta  |   |  |
|                    | integer : number of fixed effects   |  |
| nb.alpha           | integer : number of covariates in survival model  |  |
| competing_risk     | boolean : allow competing risk or not, FALSE by default   |  |
| nb.alpha.CR        | integer : number of covariates in survival model for competing risks  |  |
| variability_hetero |   |  |
|                    | boolean : allow the heterogeneous variability or not  |  |
| S                  | integer : the number of QMC points  |  |
| Zq                 | vector : sobol points   |  |
| sharedtype         | vector : dependence structure for survival model : "RE" (random effects) or "CV" (current value) or "CVS" (current value and slope) or "S" (slope)                |  |
| sharedtype_CR      | vector : dependence structure for competing risk survival model : "RE" (random effects) or "CV" (current value) or "CVS" (current value and slope) or "S" (slope) |  |

| hazard_baseline |   |
|-----------------|---|
|                 | char : baseline hazard function : "Exponential" or "Weibull" or "Splines"                           |
| hazard_baseline | _CR<br>char : baseline hazard function, competing risk : "Exponential" or "Weibull" or<br>"Splines" |
| ord.splines     | integer : the order of splines function for baseline hazard function                                |
| Xtime           | matrix : fixed effects at event time  |
| Utime           | matrix : RE at event time   |
| nb_pointsGK     | integer : number of points for Gauss-Kronrod approximation, 7 or 15 (default)                       |
| Xs              | matrix : fixed effects at Gauss-Kronrod times   |
| Us              | matrix : RE at Gauss-Kronrod times  |
| Xslope          | matrix : fixed effects of slope at event times  |
| Uslope          | matrix : RE of slope at event times   |
| Xs.slope        | matrix : fixed effects of slope at Gauss-Kronrod times  |
| Us.slope        | matrix : RE of slope at Gauss-Kronrod times   |
| indices_beta_sl |   |
|                 | vector : position of beta which will be used in the slope computation                               |
| Time            | vector : observed event times   |
| st_calc         | matrix : Gauss-Kronrod times  |
| В               | matrix : splines for baseline hazard function of event 1  |
| Bs              | matrix : splines for baseline survival function of event 1  |
| wk              | vector : Gauss-Kronrod weights  |
| Z               | matrix : covariates for survival function of event 1  |
| P               | vector : Time/2   |
| left_trunc      | boolean : left truncation indicator   |
| Z_CR            | matrix : covariates for survival function of event 2  |
| X_base          | matrix : fixed effects for longitudinal submodel  |
| offset          | vector : number of lines per subjects   |
| U               | matrix : RE for longitudinal submodel   |
| y.new.prog      | vector : y measures for longitudinal submodel   |
| event1          | vector : event 1 indicator  |
| event2          | vector : event 2 indicator  |
| Ind             | integer : number of subjects  |
| Xs.0            | same for left truncation  |
| Us.0            | same for left truncation  |
| Xs.slope.0      | same for left truncation  |
| Us.slope.0      | same for left truncation  |
| P.0             | same for left truncation  |

lsjm

| st.0          | same for left truncation   |
|---------------|--|
| Bs.0          | same for left truncation   |
| B.CR          | same for left truncation   |
| Bs.CR         | same for left truncation   |
| Bs.0.CR       | same for left truncation   |
| nb.e.a.sigma  | integer : number of RE for variability                               |
| nb.omega      | integer : number of fixed effects for variability                    |
| Otime         | matrix : fixed effects of variability at event time                  |
| Wtime         | matrix : RE of variability at event time                             |
| 0s            | matrix : fixed effects of variability at Gauss-Kronrod times         |
| Ws            | matrix : random effects of variability at Gauss-Kronrod times        |
| 0_base        | matrix : fixed effects for variability                               |
| W_base        | matrix : fixed effects for variability                               |
| correlated_re | boolean : indicator to allow all the random effects to be correlated |
| 0s.0          | matrix : same for left truncation                                    |
| Ws.0          | matrix : same for left truncation                                    |

### Value

The value of the log-likelihood

lsjm

*lsjm : Estimation of joint model for longitudinal data with a subject-specific time-dependent variability and time-to-event data.* 

### Description

This function fits complex joint models with shared random effects. The longitudinal submodel estimates longitudinal data with a mixed-effects model in which we suppose that the variance of the residual error is time-dependent and subject-specific. The survival submodel handles right-censored and left-truncated time-to-event data and competing risks. The dependence structure between the longitudinal and the survival data can be the random effects from the mixed model or the current value of the marker and/or the slope of the marker. We can also adjust on the current variance of the marker. (See below) Parameters are estimated simultaneously through a maximum likelihood method, using a Marquardt-Levenberg algorithm.

# Usage

```
lsjm(
  formFixed,
  formRandom,
  formGroup,
  formSurv,
  timeVar,
  data.long,
  variability_hetero = TRUE,
  formFixedVar,
  formRandomVar,
  correlated_re = FALSE,
  sharedtype = c("current value", "variability"),
  hazard_baseline = "Exponential",
  formSlopeFixed = NULL,
  formSlopeRandom = NULL,
  indices_beta_slope = NULL,
  nb_pointsGK = 15,
  nb.knots.splines = 1,
  competing_risk = FALSE,
  formSurv_CR = NULL,
  hazard_baseline_CR = "Exponential",
  sharedtype_CR = c("current value", "variability"),
  left_trunc = FALSE,
  Time.0 = NULL,
  S1 = 1000,
  S2 = 5000,
  nproc = 1,
  clustertype = "SOCK",
 maxiter = 100,
  print.info = FALSE,
  file = NULL,
  epsa = 0.001,
  epsb = 0.001,
  epsd = 0.001,
 binit = NULL,
  Comp.Rcpp = TRUE
```

### Arguments

)

| formFixed  | A formula for the fixed effects of the longitudinal submodel                         |
|------------|--|
| formRandom | A formula for the random effects of the longitudinal submodel                        |
| formGroup  | A formula which indicates the group variable   |
| formSurv   | A formula which indicates the variables used in the survival submodel                |
| timeVar    | The name of the column of time in data.long. This variable must appears in data.long |

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| data.long          | A dataframe with the longitudinal data  |  |
|--------------------|---|--|
| variability_het    |   |  |
| • - · · ·          | A logical to indicate if we suppose a subject_specific variability  |  |
| formFixedVar       | A formula for the fixed effects of the variance predictor   |  |
| formRandomVar      | A formula for the random effects of the variance predictor  |  |
| correlated_re      | A logical to indicate if the random effects of the marker and the variance pre-<br>dictors are correlated (By default there are supposed to be independent) |  |
| sharedtype         | char : dependence structure for survival model : "RE" (random effects) or "CV" (current value) or "CVS" (current value and slope) or "S" (slope)            |  |
| hazard_baseline    |   |  |
|                    | char : baseline hazard function : "Exponential" or "Weibull" or "Splines"   |  |
|                    | A formula for the fixed effects of the slope of the longitudinal submodel : the derivative of the formFixed   |  |
| formSlopeRandom    |   |  |
| indiana hada al    | A formula for the random effects of the slope of the longitudinal submodel : the derivative of the formRandom   |  |
| indices_beta_sl    | A vector of index indicating which beta of the formFixed formula is used in the   |  |
|                    | formSlopeFixed formula  |  |
| nb_pointsGK        | the number of points for Gauss-Kronrod approximation : choice between 7 and 15. 15 by default.  |  |
| nb.knots.spline    | 25  |  |
|                    | An integer, the number of splines for the baseline risk function (1 by default)   |  |
| competing_risk     | A logical indicating if the model handles with competing risks  |  |
| formSurv_CR        | In case of competing risk A formula which indicates the variables used in the survival submodel for the second event  |  |
| hazard_baseline_CR |   |  |
|                    | In case of competing risk : a character for the baseline hazard function of the second event  |  |
| sharedtype_CR      | In case of competing risk ; a character for the dependence structure  |  |
| left_trunc         | A logical indicating if the model handles with left truncated data  |  |
| Time.0             | In case of left truncation : a vector of entry times  |  |
| S1                 | An integer : the number of QMC draws for the first step   |  |
| S2                 | An integer : the number of QMC draws for the second step  |  |
| nproc              | An integer : the number of processors for parallel computing  |  |
| clustertype        | one of the supported types from makeCluster function  |  |
| maxiter            | optional maximum number of iterations for the marqLevAlg iterative algorithm.   |  |
| print.info         | logical indicating if the outputs of each iteration should be written   |  |
| file               | optional character giving the name of the file where the outputs of each iteration should be written (if print.info=TRUE)                                   |  |
| epsa               | optional threshold for the convergence criterion based on the parameter stability.  |  |

| epsb      | optional threshold for the convergence criterion based on the objective function stability.   |
|-----------|---|
| epsd      | optional threshold for the relative distance to maximum. This criterion has the nice interpretation of estimating the ratio of the approximation error over the statistical error, thus it can be used for stopping the iterative process whatever the problem. |
| binit     | optional initials parameters.   |
| Comp.Rcpp | boolean to indicate if the computation is performed with RCPP program or R program. True by default.  |

### Details

### A. LONGITUDINAL SUBMODEL

The longitudinal submodel is defined by a linear mixed effects model with the residual variance

|  | $Y_{ij} = Y_i(t_{ij}) = Y_i(t_{ij}) + \epsilon_{ij} = X_{ij}^{\top}\beta + Z_{ij}^{\top}b_i + \epsilon_{ij}(t_{ij}) \sim \mathcal{N}(0, \sigma_i^2(t_{ij}))  \text{with}  \log(\sigma_i(t_{ij})) = 0$ |
|--|---|
|--|---|

with  $X_{ij}$ ,  $O_{ij}$ ,  $Z_{ij}$  and  $M_{ij}$  four vectors of explanatory variables for subject *i* at visit *j*, respectively associated with the fixed-effect vectors  $\beta$  and  $\mu$ , and the subject-specific randomeffect vector *b*, and  $\tau$ , such as  $\begin{pmatrix} b_i \\ c \end{pmatrix} \approx N\left(\begin{pmatrix} 0 \\ c \end{pmatrix} \begin{pmatrix} \Sigma_b & \Sigma_{\tau b} \end{pmatrix}\right)$ .

effect vector 
$$b_i$$
 and  $\tau_i$ , such as  $\begin{pmatrix} 0_i \\ \tau_i \end{pmatrix} \sim N\left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} 2_0 & 2_{7b} \\ \Sigma'_{\tau b} & \Sigma_{\tau} \end{pmatrix}\right)$ 

$$Y_i(t_{ij}) = Y_i(t_{ij}) + \epsilon_{ij} = X_{ij}^{\dagger}\beta + Z_{ij}^{\dagger}b_i + \epsilon_{ij}$$

with  $X_{ij}$  and  $Z_{ij}$  two covariate vectors for subject i at visit j, respectively associated with the vector of fixed effects  $\beta$  and the vector of subject-specific individual random effects  $b_i$ . The vector  $b_i$  is assumed to be normally distributed and a specific-subject random effect on the variance of the measure error can be added:  $\epsilon_{ij} \sim \mathcal{N}(0, \sigma_i^2)$  and

$$\begin{pmatrix} b_i \\ \log \sigma_i \end{pmatrix} \sim \mathcal{N} \left( \begin{pmatrix} 0 \\ \mu_{\sigma} \end{pmatrix}, \begin{pmatrix} \Sigma_b & 0 \\ 0 & \tau_{\sigma}^2 \end{pmatrix} \right)$$
  
B. SURVIVAL SUBMODEL

The risk function for the event  $k = \{1,2\}$  is defined by:  $\lambda_{ik}(t) = \lambda_{0k}(t) \exp\left(W_i^{\top} \gamma_k + \alpha_{1k} \tilde{y}_i(t) + \alpha_{2k} \tilde{y}'_i(t) + \alpha_{\sigma k} \sigma_i(t)\right)$ with  $\lambda_{0k}(t)$  the baseline risk function,  $W_i$  a vector of baseline covariates associated with the regression coefficient  $\gamma_k$ , and  $\alpha_{1k}$ ,  $\alpha_{2k}$  and  $\alpha_{\sigma k}$  the regression coefficients associated with the current value  $\tilde{y}_i(t)$ , the current slope  $\tilde{y}'_i(t)$  and the current variability  $\sigma_i(t)$  of the marker, respectively. Different parametric forms for the baseline risk function can be considered, such as exponential, Weibull, or, for more flexibility, a B-splines base.

### Value

A FlexVarJoint object which contains the following elements :

result A marqLevAlg object with the results of the estimation.

table.res The table of results : Estimation and SE

time.compute Computation time

control A list of control elements

lsmm

### Examples

```
#fit a joint model with competing risks and subject-specific variability
example <- lsjm(formFixed = y~visit,</pre>
formRandom = ~ visit,
formGroup = \simID,
formSurv = Surv(time, event ==1 ) ~ 1,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
sharedtype = c("current value", "variability"),
hazard_baseline = "Weibull",
formSlopeFixed =~1,
formSlopeRandom = \sim 1,
indices_beta_slope = c(2),
competing_risk = TRUE,
formSurv_CR = Surv(time, event ==2 ) ~ 1,
hazard_baseline_CR = "Weibull",
sharedtype_CR = c("current value", "variability"),
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100,
Comp.Rcpp = TRUE
)
summary(example)
```

lsmm

*lsmm* : Estimation of location scale mixed model

### Description

This function fits complex mixed effects model with a time and covariate dependent variance. We suppose that the variance of the residual error is time-dependent and subject-specific. Parameters are estimated simultaneously through a maximum likelihood method, using a Marquardt-Levenberg algorithm.

### Usage

lsmm(

lsmm

```
formFixed,
formRandom,
formGroup,
timeVar,
data.long,
variability_hetero = TRUE,
formFixedVar,
formRandomVar,
correlated_re = FALSE,
S1 = 1000,
S2 = 5000,
nproc = 1,
clustertype = "SOCK",
maxiter = 100,
print.info = FALSE,
file = NULL,
epsa = 0.001,
epsb = 0.001,
epsd = 0.001,
binit = NULL
```

# Arguments

)

| formFixed      | A formula for the fixed effects of the longitudinal submodel  |
|----------------|---|
| formRandom     | A formula for the random effects of the longitudinal submodel   |
| formGroup      | A formula which indicates the group variable  |
| timeVar        | The name of the column of time in data.long. This variable must appears in data.long  |
| data.long      | A dataframe with the longitudinal data  |
| variability_he | tero  |
|                | A logical to indicate if we suppose a subject_specific variability  |
| formFixedVar   | A formula for the fixed effects of the variance predictor   |
| formRandomVar  | A formula for the random effects of the variance predictor  |
| correlated_re  | A logical to indicate if the random effects of the marker and the variance pre-<br>dictors are correlated (By default there are supposed to be independent) |
| S1             | An integer : the number of QMC draws for the first step   |
| S2             | An integer : the number of QMC draws for the second step  |
| nproc          | An integer : the number of processors for parallel computing  |
| clustertype    | one of the supported types from makeCluster function  |
| maxiter        | optional maximum number of iterations for the marqLevAlg iterative algorithm.   |
| print.info     | logical indicating if the outputs of each iteration should be written   |
| file           | optional character giving the name of the file where the outputs of each iteration should be written (if print.info=TRUE)                                   |

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| epsa  | optional threshold for the convergence criterion based on the parameter stability.  |
|-------|---|
| epsb  | optional threshold for the convergence criterion based on the objective function stability.   |
| epsd  | optional threshold for the relative distance to maximum. This criterion has the nice interpretation of estimating the ratio of the approximation error over the statistical error, thus it can be used for stopping the iterative process whatever the problem. |
| binit | optional initials parameters.   |

#### Details

The model is defined by : #'  $\begin{cases} Y_{ij} = Y_i(t_{ij}) = \widetilde{Y}_i(t_{ij}) + \epsilon_{ij} = X_{ij}^\top \beta + Z_{ij}^\top b_i + \epsilon_{ij}, \\ \epsilon_{ij}(t_{ij}) \sim \mathcal{N}(0, \sigma_i^2(t_{ij})) & \text{with} \quad \log(\sigma_i(t_{ij})) = O_{ij}^\top \mu + M_{ij}^\top \tau_i \end{cases}$ 

with  $X_{ij}$ ,  $O_{ij}$ ,  $Z_{ij}$  and  $M_{ij}$  four vectors of explanatory variables for subject i at visit j, respectively associated with the fixed-effect vectors  $\beta$  and  $\mu$ , and the subject-specific randomeffect vector  $b_i$  and  $\tau_i$ , such as  $\begin{pmatrix} b_i \\ \tau_i \end{pmatrix} \sim N\left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \Sigma_b & \Sigma_{\tau b} \\ \Sigma'_{\tau b} & \Sigma_{\tau} \end{pmatrix}\right)$ :  $Y_i(t_{ij}) = \tilde{Y}_i(t_{ij}) + \epsilon_{ij} = X_{ij}^{\top}\beta + Z_{ij}^{\top}b_i + \epsilon_{ij}$ 

with  $X_{ij}$  and  $Z_{ij}$  two covariate vectors for subject i at visit j, respectively associated with the vector of fixed effects  $\beta$  and the vector of subject-specific individual random effects  $b_i$ . The vector  $b_i$  is assumed to be normally distributed and a specific-subject random effect on the variance of the measure error can be added:  $\epsilon_{ij} \sim \mathcal{N}(0, \sigma_i^2)$  and

$$\begin{pmatrix} b_i \\ \log \sigma_i \end{pmatrix} \sim \mathcal{N}\left(\begin{pmatrix} 0 \\ \mu_{\sigma} \end{pmatrix}, \begin{pmatrix} \Sigma_b & 0 \\ 0 & \tau_{\sigma}^2 \end{pmatrix}\right)$$

### Value

A FlexVarJoint object which contains the following elements :

result A marqLevAlg object with the results of the estimation.

table.res The table of results : Estimation and SE

time.compute Computation time

control A list of control elements

### Examples

```
#fit a joint model with competing risks and subject-specific variability
example <- lsmm(formFixed = y~visit,
formRandom = ~ visit,
formGroup = ~ID,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,</pre>
```

predyn

```
formRandomVar =~visit,
correlated_re = TRUE,
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100
)
summary(example)
```

predyn

### Dynamic prediction for new individuals

# Description

Dynamic prediction for new individuals

# Usage

```
predyn(
    newdata,
    object,
    s,
    times,
    event = 1,
    IC = 95,
    nb.draws = 500,
    graph = FALSE
)
```

# Arguments

| newdata  | data frame : collected data for a new individual   |
|----------|--|
| object   | lsjm object : estimation of the model  |
| S        | numeric : the time to begin prediction   |
| times    | numeric vector : future times to calculate predictions   |
| event    | integer $(0, 1 \text{ or } 2)$ : the event of interest for the prediction  |
| IC       | integer : percentage of confidence for the interval confidence (between 0 and 100), 95 by default, NULL if no IC |
| nb.draws | integer : the number of simulations to compute the interval confidence (by bootstrap), 500 by default            |
| graph    | boolean : indicator to plot the graphs or not  |

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### Value

A table of dynamic predictions

### Examples

```
#fit a joint model with competing risks and subject-specific variability
example <- lsjm(formFixed = y~visit,</pre>
formRandom = ~ visit,
formGroup = \simID,
formSurv = Surv(time, event ==1 ) ~ 1,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
sharedtype = c("current value", "variability"),
hazard_baseline = "Weibull",
formSlopeFixed =~1,
formSlopeRandom = ~1,
indices_beta_slope = c(2),
competing_risk = TRUE,
formSurv_CR = Surv(time, event ==2 ) ~ 1,
hazard_baseline_CR = "Weibull",
sharedtype_CR = c("current value", "variability"),
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100,
Comp.Rcpp = TRUE
)
#Prediction for individuals 1 and 3 to experiment the event 1
#at time 1.5, 2, and 3, given their measurements until time 1:
newdata <- Data_toy[which(Data_toy$ID %in% c(1,3)),]</pre>
pred.new <- predyn(newdata,example,1, c(1.5,2,2.8,3), event = 1, IC = 95,</pre>
nb.draws = 100, graph = TRUE)
```

pred\_s.t.bootstrap.tps

Predictions computation

### Description

Predictions computation

# Usage

```
pred_s.t.bootstrap.tps(newdata, object, s, window, event = 1, nb.draws)
```

### Arguments

| newdata  | data frame : collected data for a new individual                          |
|----------|---|
| object   | lsjm object : estimation of the model                                     |
| S        | numeric : the time to begin prediction                                    |
| window   | numeric : the side of the prediction window                               |
| event    | integer $(0, 1 \text{ or } 2)$ : the event of interest for the prediction |
| nb.draws | integer : the number of draws to compute the IC                           |

pred\_s.t.ponctuel.tps Predictions computation

# Description

Predictions computation

# Usage

```
pred_s.t.ponctuel.tps(newdata, object, s, window, event = 1)
```

### Arguments

| newdata | data frame : collected data for a new individual                          |
|---------|---|
| object  | lsjm object : estimation of the model                                     |
| S       | numeric : the time to begin prediction                                    |
| window  | numeric : the side of the prediction window                               |
| event   | integer $(0, 1 \text{ or } 2)$ : the event of interest for the prediction |

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